

1- Prove the law of cosines for a triangle.

$$C = \sqrt{A^2 + B^2 - 2AB \cos \alpha}$$

2- Given three vectors \mathbf{A} , \mathbf{B} , and \mathbf{C} , obtain the expressions of (a) $\mathbf{A} \cdot \mathbf{B}$, (b) $\mathbf{A} \times \mathbf{B}$, and (c) $\mathbf{C} \cdot (\mathbf{A} \times \mathbf{B})$ in the orthogonal curvilinear coordinate system (u_1, u_2, u_3). $\mathbf{A} = A_1 u_1 + A_2 u_2 + A_3 u_3$, $\mathbf{B} = B_1 u_1 + B_2 u_2 + B_3 u_3, \dots$

3- (a) Write the expression of the vector going from point $P_1 = (1, 2, -1)$ to point $P_2 = (3, -2, -4)$ in Cartesian coordinates. (b) What is the length of this line?

4- Express the vector $\mathbf{A} = a_r (2 \cos \varphi) - a_\varphi 2r + a_z 2$ in Cartesian coordinates.

5- The position of a point P in spherical coordinates is $(8, 120^\circ, 330^\circ)$. Specify its location (determine the vector: \mathbf{OP}) (a) in Cartesian coordinates, and (b) in cylindrical coordinates.

6- Determine the values of the following products of base vectors:

a) $a_x \cdot a_\varphi$ b) $a_\theta \cdot a_y$ c) $a_r \times a_x$

d) $a_R \cdot a_r$ e) $a_y \cdot a_R$ f) $a_R \cdot a_z$

g) $a_R \times a_z$ h) $a_\theta \cdot a_z$ i) $a_z \times a_\theta$

7- Find the component of the vector $\mathbf{A} = -a_y z + a_z y$ at the point $P_1 (0, -2, 3)$, which is directed toward the point $P_2(\sqrt{3} - 60^\circ, 1)$.

(در واقع تصویر بردار \mathbf{A} روی بردار $P_1 P_2$ خواسته شده و مشخص است که نقطه اول دکارتی و دومی استوانه ای داده شده است.)