

بسمه تعالی

فرمول های درس فیزیک الکترونیک (مخصوص جلسه امتحان)

۱- پاسخ عمومی معادله دیفرانسیل $\frac{d^2y}{dx^2} - a^2y = 0$ به صورت $y = C_1e^{-ax} + C_2e^{ax}$ می باشد.

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$$\begin{aligned} \chi_{Si} &= 4.05\text{eV} & \phi_{Ni} &= 4.5\text{eV} \\ (E_g)_{Si} &= 1.1\text{eV} & (n_i)_{Si} &= 1.45 \times 10^{10} \text{ cm}^{-3} \\ (E_g)_{GaAs} &= 1.42 \text{ eV} & (n_i)_{GaAs} &= 2.1 \times 10^6 \text{ cm}^{-3} \end{aligned}$$

۳- برای سیلیکن (اگر در متن سؤال داده نشده باشد):

$$D_p = 12.5 \text{ cm}^2/\text{s} \quad D_n = 35 \text{ cm}^2/\text{s} \quad \mu_n = 1500 \text{ cm}^2/\text{V-s} \quad \mu_p = 450 \text{ cm}^2/\text{V-s}$$

$$\tau_n = \tau_p = 2 \mu\text{s}$$

۴- برخی ثابتهای بنیادی عبارتند از:

$$N_{av} = 6.02 \times 10^{23} / \text{mol} \quad \text{عدد آووگادرو}$$

$$k = 1.38 \times 10^{-23} \text{ J/K} \quad \text{ثابت بولتزمن}$$

$$q = 1.6 \times 10^{-19} \text{ C} \quad \text{بار الکترون}$$

$$h = 6.63 \times 10^{-34} \text{ J-s} \quad \text{ثابت پلانک}$$

$$\epsilon_0 = 8.85 \times 10^{-14} \text{ F/cm} \quad \text{و}$$

$$\epsilon_r(\text{Si}) \approx 11.8$$

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	Si	GaAs
N_V	$9.84 \times 10^{18} \text{ cm}^{-3}$	$7.72 \times 10^{18} \text{ cm}^{-3}$
N_C	$2.78 \times 10^{19} \text{ cm}^{-3}$	$4.45 \times 10^{17} \text{ cm}^{-3}$

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$$\begin{aligned} \sinh x &= \frac{e^x - e^{-x}}{2} & \cosh x &= \frac{e^x + e^{-x}}{2} \\ \tanh x &= \frac{\sinh x}{\cosh x} = \frac{e^x - e^{-x}}{e^x + e^{-x}} & \coth x &= \frac{\cosh x}{\sinh x} = \frac{e^x + e^{-x}}{e^x - e^{-x}} \\ \operatorname{sech} x &= \frac{1}{\cosh x} = \frac{2}{e^x + e^{-x}} & \operatorname{csch} x &= \frac{1}{\sinh x} = \frac{2}{e^x - e^{-x}} \end{aligned}$$

SEMICONDUCTOR PHYSICS

Electron Momentum: $\mathbf{p} = m\mathbf{v} = \hbar\mathbf{k} = \frac{\hbar}{\lambda}$

Planck: $E = h\nu = \hbar\omega$

Kinetic: $E = \frac{1}{2}mv^2 = \frac{1}{2} \frac{\hbar^2}{m} \mathbf{k}^2$ (3-4)

Effective mass: $m^* = \frac{\hbar^2}{d^2E/d\mathbf{k}^2}$ (3-3)

Total electron energy = $P.E. + K.E. = E_c + E(\mathbf{k})$

Fermi-Dirac e^- distribution: $f(E) = \frac{1}{e^{(E-E_F)/kT} + 1} \cong e^{-(E-E_F)/kT}$ for $E \gg E_F$ (3-10)

Equilibrium: $n_0 = \int_{-E_c}^{\infty} f(E)N(E)dE = N_c f(E_c) = N_c e^{-(E_c-E_F)/kT}$ (3-15)

$N_c = 2 \left(\frac{2\pi m_n^* kT}{h^2} \right)^{3/2}$ (3-16), (3-20)

$p_0 = N_v [1 - f(E_v)] = N_v e^{-(E_v-E_F)/kT}$ (3-19)

$n_i = N_c e^{-(E_c-E_i)/kT}$, $p_i = N_v e^{-(E_i-E_v)/kT}$ (3-21)

$n_i = \sqrt{N_c N_v} e^{-E_i/2kT} = 2 \left(\frac{2\pi kT}{h^2} \right)^{3/2} (m_n^* m_p^*)^{3/4} e^{-E_i/2kT}$ (3-23), (3-26)

Equilibrium: $\frac{n_0}{p_0} = n_i e^{(E_F-E_i)/kT}$ (3-25) $n_0 p_0 = n_i^2$ (3-24)

Steady state: $\frac{n}{p} = N_c e^{-(E_c-F_n)/kT} = n_i e^{(F_n-E_i)/kT}$ (4-15) $np = n_i^2 e^{(F_n-F_p)/kT}$ (5-38)

$\mathcal{E}(x) = -\frac{dV(x)}{dx} = \frac{1}{q} \frac{dE_i}{dx}$ (4-26)

Poisson: $\frac{d\mathcal{E}(x)}{dx} = -\frac{d^2V(x)}{dx^2} = \frac{\rho(x)}{\epsilon} = \frac{q}{\epsilon} (p - n + N_d^+ - N_a^-)$ (5-14)

$\mu \cong \frac{q\ell}{m^*}$ (3-40a) Drift: $v_d \cong \frac{\mu \mathcal{E}}{1 + \mu \mathcal{E}/v_s} \left\{ \begin{array}{l} = \mu \mathcal{E} \text{ (low fields, ohmic)} \\ = v_s \text{ (high fields, saturated vel.)} \end{array} \right.$ (Fig. 6-9)

Drift current density: $\frac{I_x}{A} = J_x = q(n\mu_n + p\mu_p)\mathcal{E}_x = \sigma \mathcal{E}_x$ (3-43)

$J_n(x) = q\mu_n n(x)\mathcal{E}(x) + qD_n \frac{dn(x)}{dx}$

Conduction Current: drift diffusion (4-23)

$J_p(x) = q\mu_p p(x)\mathcal{E}(x) - qD_p \frac{dp(x)}{dx}$

$J_{\text{total}} = J_{\text{conduction}} + J_{\text{displacement}} = J_n + J_p + C \frac{dV}{dt}$

Continuity: $\frac{\partial p(x,t)}{\partial t} = -\frac{1}{q} \frac{\partial J_p}{\partial x} - \frac{\delta p}{\tau_p} \quad \frac{\partial n}{\partial t} = \frac{1}{q} \frac{\partial J_n}{\partial x} - \frac{\delta n}{\tau_n}$ (4-31)

For steady state diffusion: $\frac{d^2 \delta n}{dx^2} = \frac{\delta n}{D_n \tau_n} \equiv \frac{\delta n}{L_n^2}$ $\frac{d^2 \delta p}{dx^2} = \frac{\delta p}{L_p^2}$ (4-34)

Diffusion length: $L \equiv \sqrt{D\tau}$ Einstein relation: $\frac{D}{\mu} = \frac{kT}{q}$ (4-29)

p-n JUNCTIONS

Equilibrium: $V_0 = \frac{kT}{q} \ln \frac{p_p}{p_n} = \frac{kT}{q} \ln \frac{N_a}{n_i^2/N_d} = \frac{kT}{q} \ln \frac{N_a N_d}{n_i^2}$ (5-8)

$\frac{p_p}{p_n} = \frac{n_n}{n_p} = e^{qV_0/kT}$ (5-10) $W = \left[\frac{2\epsilon(V_0 - V)}{q} \left(\frac{N_a + N_d}{N_a N_d} \right)^{1/2} \right]$ (5-57)

One-sided abrupt p^+n : $x_{n0} = \frac{WN_a}{N_a + N_d} \cong W$ (5-23) $V_0 = \frac{qN_d W^2}{2\epsilon}$

$\Delta p_n = p(x_{n0}) - p_n = p_n (e^{qV/kT} - 1)$ (5-29)

$\delta p(x_n) = \Delta p_n e^{-x_n/L_p} = p_n (e^{qV/kT} - 1) e^{-x_n/L_p}$ (5-31b)

Ideal diode: $I = qA \left(\frac{D_p}{L_p} p_n + \frac{D_n}{L_n} n_p \right) (e^{qV/kT} - 1) = I_0 (e^{qV/kT} - 1)$ (5-36)

Non-ideal: $I = I_0 (e^{qV/mkT} - 1)$ ($n = 1$ to 2) (5-74)

With light: $I_{\text{op}} = qA g_{\text{op}} (L_p + L_n + W)$ (8-1)

$$\text{Capacitance: } C = \left| \frac{dQ}{dV} \right| \quad (5-55)$$

$$\text{Junction Depletion: } C_j = \epsilon A \left[\frac{q}{2\epsilon(V_0 - V)} \frac{N_d N_a}{N_d + N_a} \right]^{1/2} = \frac{\epsilon A}{W} \quad (5-62)$$

$$\text{Stored charge exp. hole dist.: } Q_p = qA \int_0^\infty \delta p(x_n) dx_n = qA \Delta p_n \int_0^\infty e^{-x_n/L_p} dx_n = qAL_p \Delta p_n \quad (5-39)$$

$$I_p(x_n = 0) = \frac{Q_p}{\tau_p} = qA \frac{L_p}{\tau_p} \Delta p_n = qA \frac{D_p}{L_p} p_n (e^{qV/kT} - 1) \quad (5-40)$$

$$G_s = \frac{dI}{dV} = \frac{qAL_p p_n}{\tau_p} \frac{d}{dV} (e^{qV/kT}) = \frac{q}{kT} I \quad (5-67c)$$

$$\text{Long } p^+ \text{-n: } i(t) = \frac{Q_p(t)}{\tau_p} + \frac{dQ_p(t)}{dt} \quad (5-47)$$

MOS-n CHANNEL

$$\text{Oxide: } C_i = \frac{\epsilon_i}{d} \quad \text{Depletion: } C_d = \frac{\epsilon_s}{W} \quad \text{MOS: } C = \frac{C_i C_d}{C_i + C_d} \quad (6-36)$$

$$\text{Threshold: } V_T = \Phi_{ms} - \underbrace{\frac{Q_i}{C_i} - \frac{Q_d}{C_d}}_{C_i} + 2\phi_F \quad (6-38)$$

Flat band

$$\text{Inversion: } \phi_s (\text{inv.}) = 2\phi_F = 2 \frac{kT}{q} \ln \frac{N_a}{n_i} \quad (6-15) \quad W = \left[\frac{2\epsilon_s \phi_s}{qN_a} \right]^{1/2} \quad (6-30)$$

$$Q_d = -qN_a W_m = -2(\epsilon_s q N_a \phi_F)^{1/2} \quad (6-32) \quad \text{At } V_{FB}: C_{FB} = \frac{C_i C_{\text{debye}}}{C_i + C_{\text{debye}}}$$

$$\text{Debye screening length: } L_D = \sqrt{\frac{\epsilon_s kT}{q^2 P_0}} \quad (6-25) \quad C_{\text{debye}} = \frac{\sqrt{2} \epsilon_s}{L_D} \quad (6-40)$$

$$\text{Substrate bias: } \Delta V_T \approx \frac{\sqrt{2\epsilon_s q N_a}}{C_i} (-V_B)^{1/2} \quad (\text{n channel}) \quad (6-63)$$

$$I_D = \frac{\bar{\mu}_n Z C_i}{L} \left\{ (V_G - V_{FB} - 2\phi_F - \frac{1}{2}V_D)V_D - \frac{2}{3} \frac{\sqrt{2\epsilon_s q N_a}}{C_i} [(V_D + 2\phi_F)^{3/2} - (2\phi_F)^{3/2}] \right\} \quad (6-50)$$

$$I_D \approx \frac{\bar{\mu}_n Z C_i}{L} [(V_G - V_T)V_D - \frac{1}{2}V_D^2] \quad (6-49)$$

$$\text{Saturation: } I_D(\text{sat.}) \approx \frac{1}{2} \bar{\mu}_n C_i \frac{Z}{L} (V_G - V_T)^2 = \frac{Z}{2L} \bar{\mu}_n C_i V_D^2(\text{sat.}) \quad (6-53)$$

$$g_m = \frac{\partial I_D}{\partial V_G}; \quad g_m(\text{sat.}) = \frac{\partial I_D(\text{sat.})}{\partial V_G} \approx \frac{Z}{L} \bar{\mu}_n C_i (V_G - V_T) \quad (6-54)$$

$$\text{For short } L: \quad I_D \approx ZC_i(V_G - V_T)v_s \quad (6-60)$$

$$\text{Subthreshold slope: } S = \frac{dV_G}{d(\log I_D)} = \frac{kT}{q} \ln 10 \left[1 + \frac{C_d + C_i}{C_i} \right] \quad (6-66)$$

BJT-p-n-p

$$I_{Ep} = qA \frac{D_p}{L_p} \left(\frac{W_b}{L_p} \text{csch} \frac{W_b}{L_p} - \Delta p_C \text{csch} \frac{W_b}{L_p} \right) \quad (7-18) \quad \Delta p_E = P_n (e^{qV_{EB}/kT} - 1)$$

$$\Delta p_C = P_n (e^{qV_{CB}/kT} - 1) \quad (7-8)$$

$$I_C = qA \frac{D_p}{L_p} \left(\Delta p_E \text{csch} \frac{W_b}{L_p} - \Delta p_C \text{cosh} \frac{W_b}{L_p} \right)$$

$$I_B = qA \frac{D_p}{L_p} \left[(\Delta p_E + \Delta p_C) \tanh \frac{W_b}{2L_p} \right] \quad (7-19)$$

$$B = \frac{I_C}{I_E} = \frac{\text{csch} \frac{W_b/L_p}{L_p}}{\text{cosh} \frac{W_b/L_p}{L_p}} = \text{sech} \frac{W_b}{L_p} \approx 1 - \left(\frac{W_b}{2L_p} \right)^2 \quad (7-26)$$

(Base transport factor)

$$\gamma = \frac{I_{Ep}}{I_{En} + I_{Ep}} = \left[1 + \frac{L_p^n \mu_n \mu_p \tanh \frac{W_b}{L_p}}{L_p^n \mu_p \mu_n} \right]^{-1} \approx \left[1 + \frac{W_b^2 \mu_n \mu_p}{L_p^2 \mu_p \mu_n} \right]^{-1} \quad (7-25)$$

(Emitter injection efficiency)

$$\frac{i_C}{i_E} = B\gamma \equiv \alpha \quad (7-3) \quad \frac{i_C}{i_B} = \frac{B\gamma}{1 - B\gamma} = \frac{\alpha}{1 - \alpha} \equiv \beta \quad (7-6) \quad \frac{i_C}{i_B} = \beta = \frac{\tau_p}{\tau_n} \quad (7-7)$$

(Common base gain) (Common emitter gain) (For $\gamma = 1$)